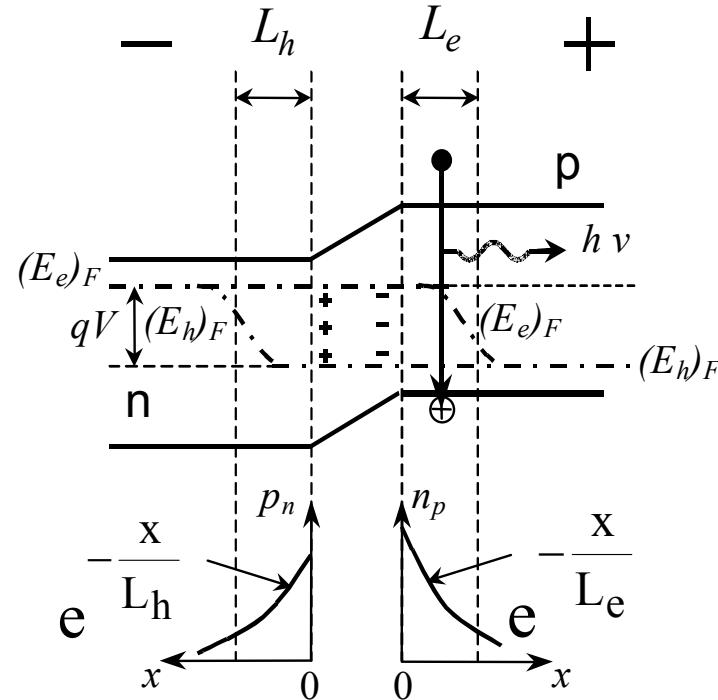
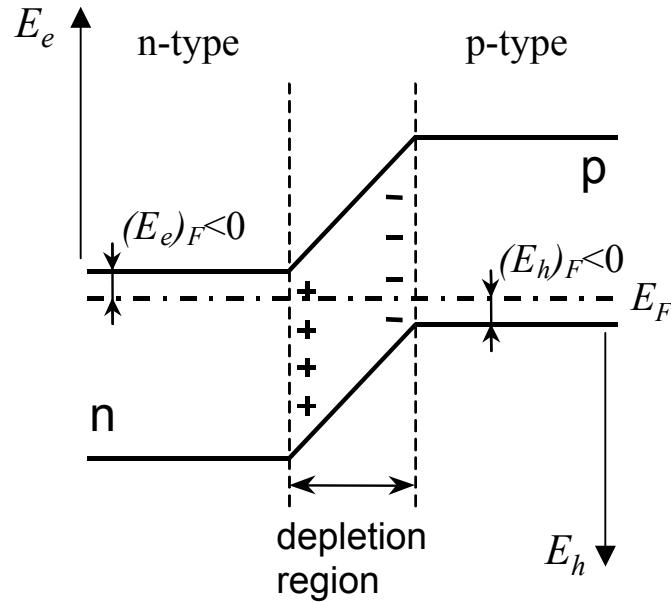


Emission in p-n homojunction

1. Weak doping



Diffusion length of electrons and holes in n and p-type regions

$$L_e = \sqrt{(D_e)_p (\tau_e)_p}$$

$$L_h = \sqrt{(D_h)_n (\tau_h)_n}$$

$$n_p = (n_p)_0 + \Delta n_p \approx \Delta n_p = \Delta p_p$$

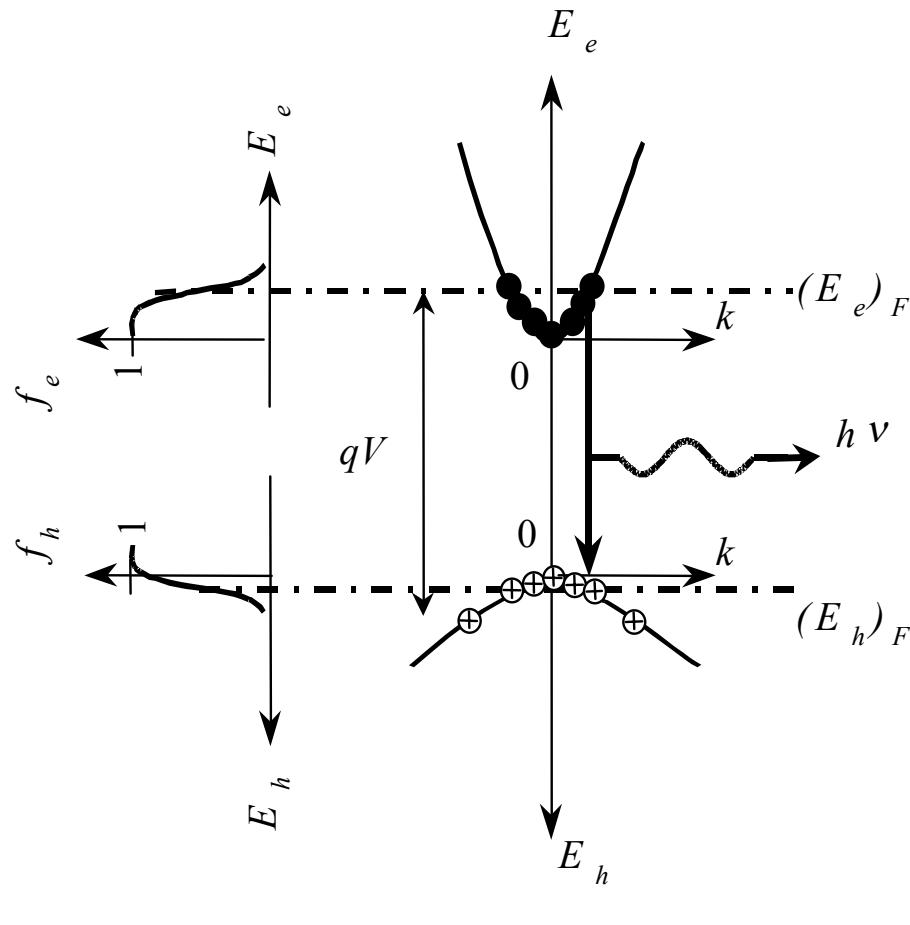
$$p_n = (p_n)_0 + \Delta p_n \approx \Delta p_n = \Delta n_n$$

$(D_e)_p, (D_h)_n$ are diffusion coefficients of electrons in p-type region and holes in n-type region

$(\tau_e)_p, (\tau_h)_n$ are lifetimes of electrons and holes in p-type and n-type regions accordingly

Emission in p-n homojunction

1. Heavy doping. Amplification of light.



Amplification (population inversion) condition

$$f_e(E_e) + f_h(E_h) > 1$$

$$f_e(E_e) > 1 - f_h(E_h)$$

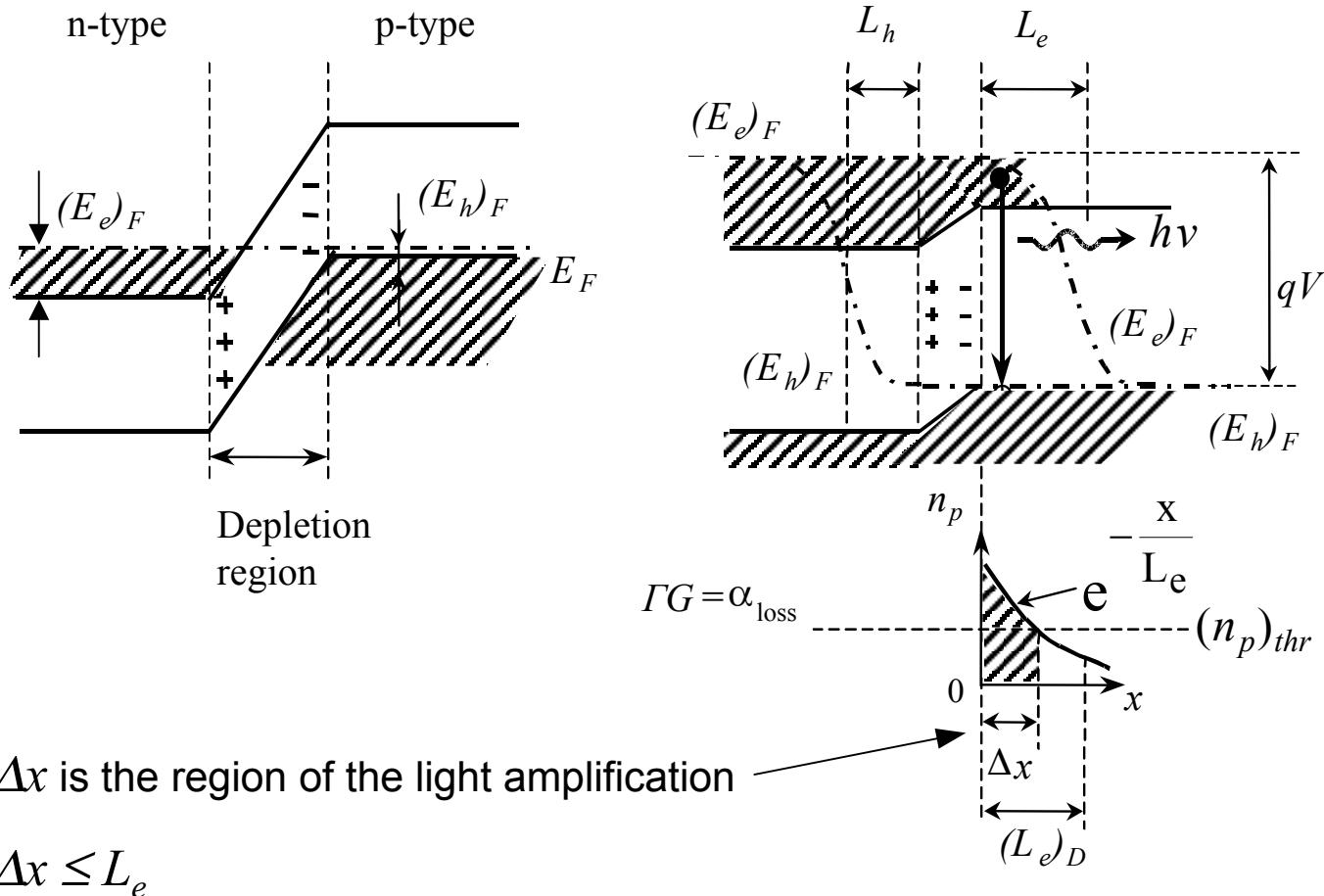
$$f_e^{CB}(E_e) > f_e^{VB}(E_h)$$

can be rewritten as

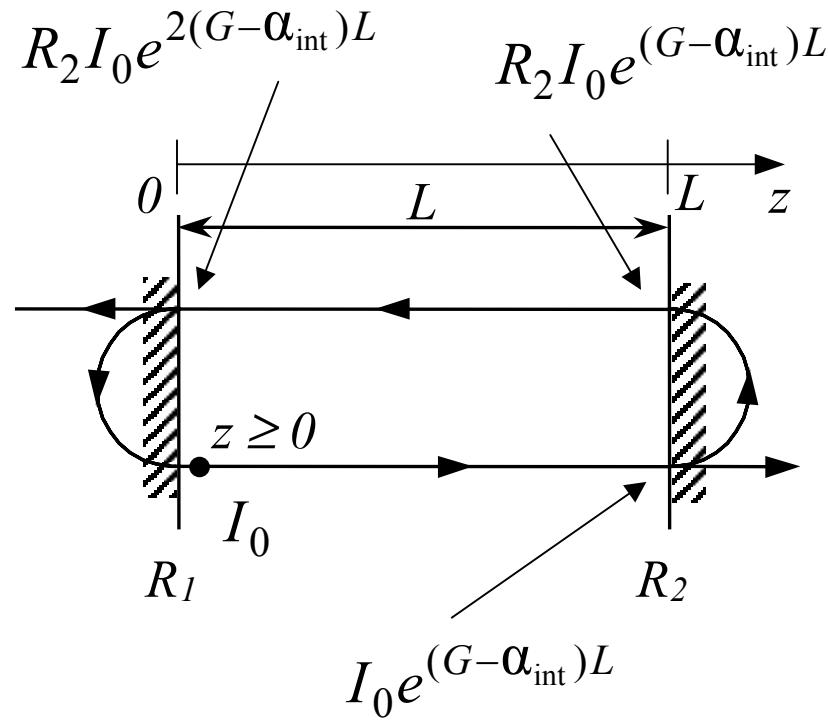
$$\exp\left[\frac{(qV - h\nu)}{k_B T}\right] > 1$$

Emission in p-n homojunction

2. Heavy doping. Amplification of light.



Threshold condition for lasing



$$1. \quad I_o e^{(G-\alpha_{\text{int}})L} R_2 e^{(G-\alpha_{\text{int}})L} R_1 \geq I_o$$

$$G = \alpha_{\text{int}} + \frac{1}{2L} \ln \frac{1}{R_1 R_2} = \alpha_{\text{int}} + \alpha_m = \alpha_{\text{loss}}$$

α_{int} – internal loss (mainly due to free carrier absorption)

α_m – mirror loss (reflection is less than 100%)

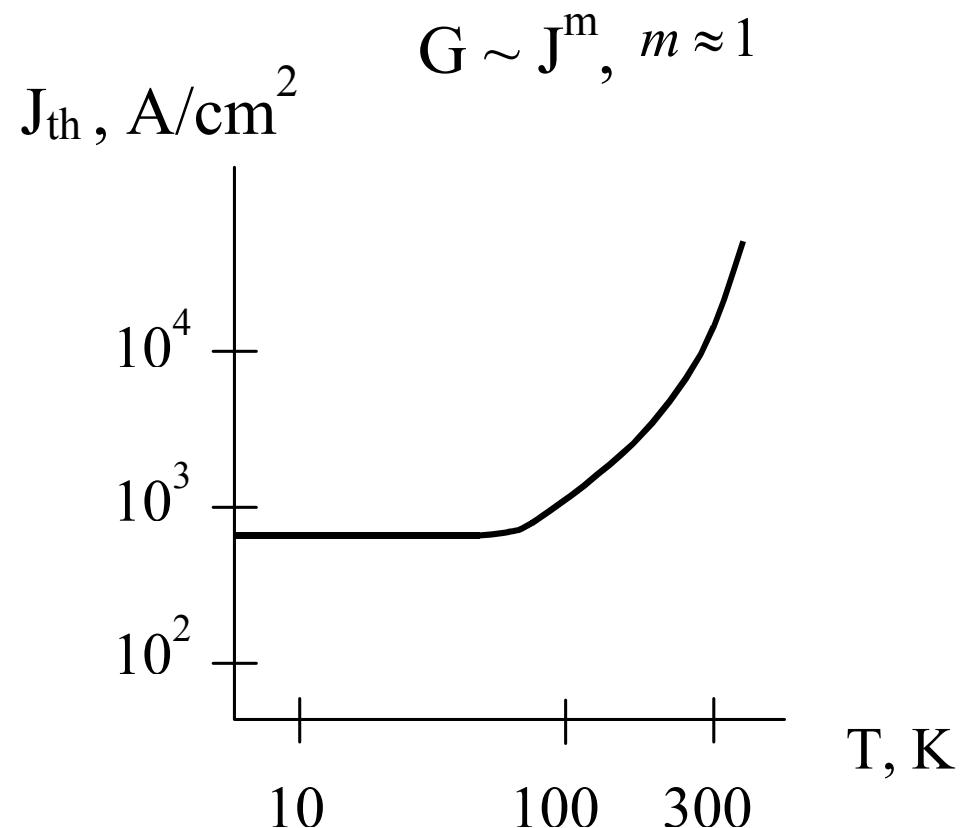
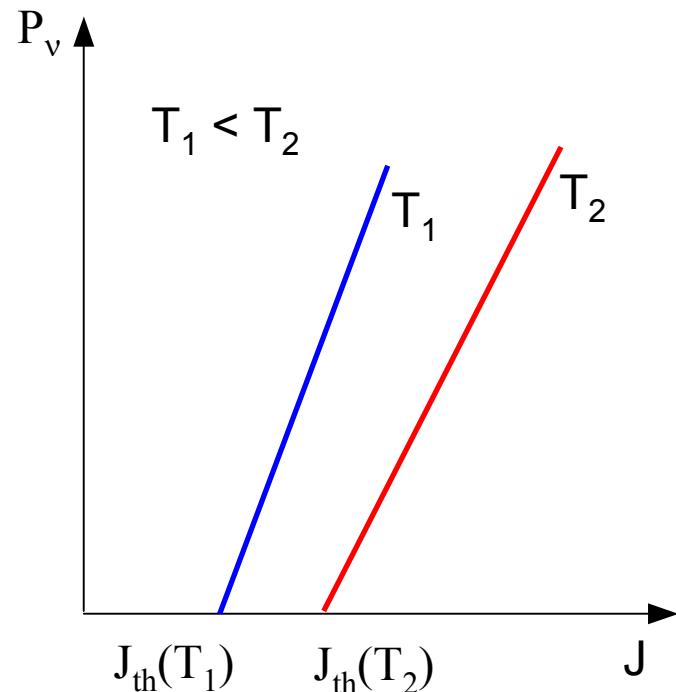
In the waveguide: $\Gamma G = g = \alpha_{\text{loss}}$, g is modal gain, Γ is optical confinement

$\Gamma \approx \Delta x/d$, Δx – region of amplification, d – waveguide thickness ($d \approx \lambda/n$)

$$2. \quad \frac{2L}{\lambda/n} = m, \quad m = 1, 2, \dots \quad m \gg 1 \quad \nu_{m+1} - \nu_m = \Delta \nu = \frac{c}{2Ln}$$

Emission in p-n homojunction

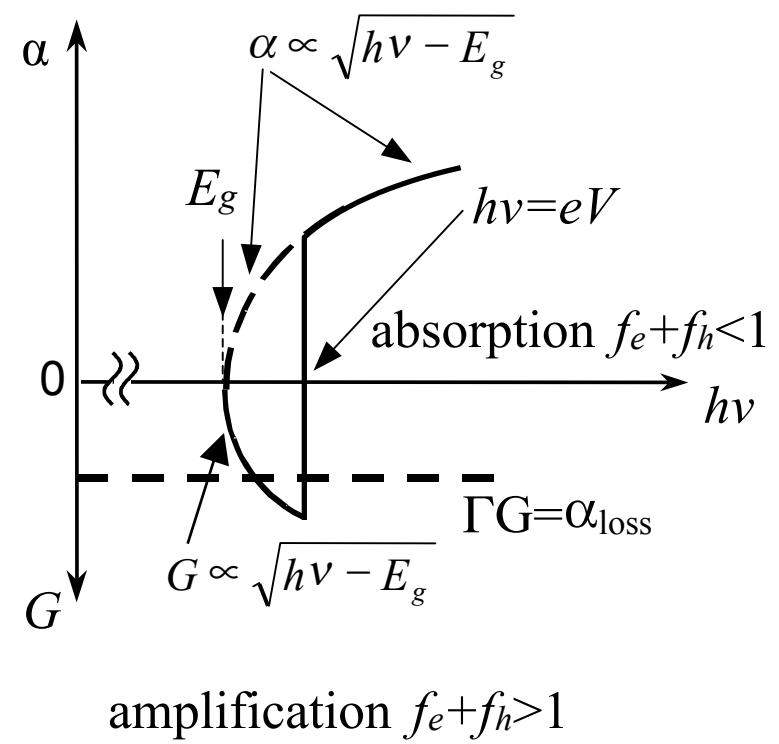
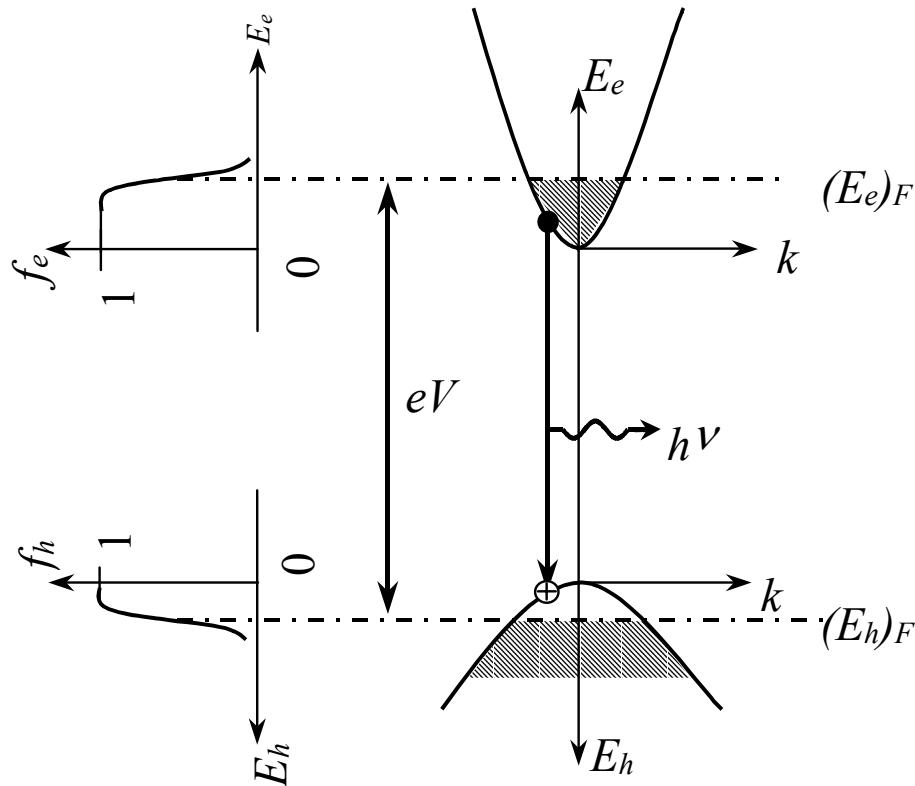
Why does j_{th} increase with increasing T?
 The main reason is change of distribution function with T.



Emission in p-n homojunction

Temperature dependence of the threshold current or gain

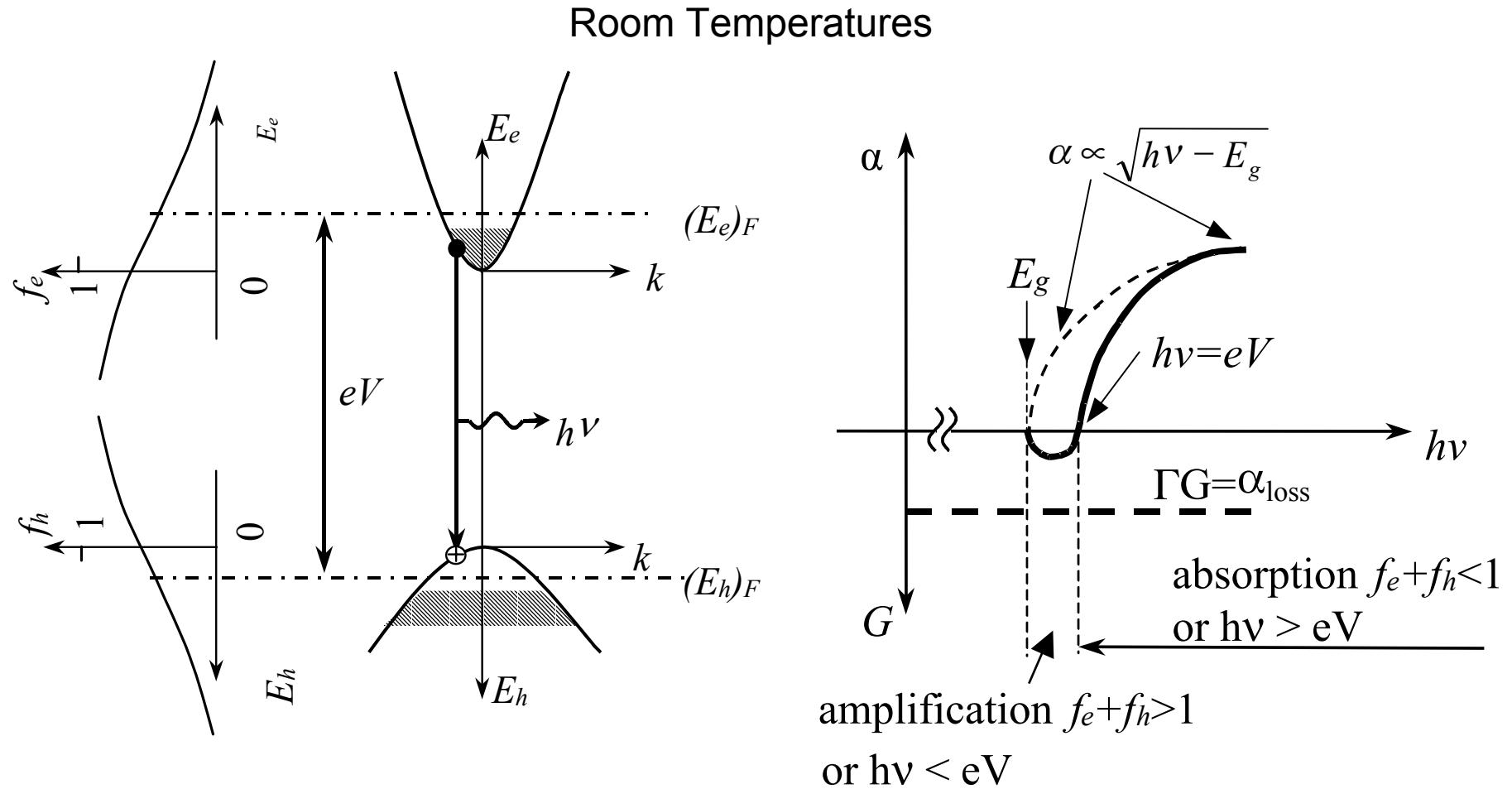
Low Temperatures, $T \sim 0\text{K}$



Gain can overcome losses and generation is possible

Emission in p-n homojunction

Temperature dependence of the threshold current or gain



Gain can not overcome losses and generation is not possible