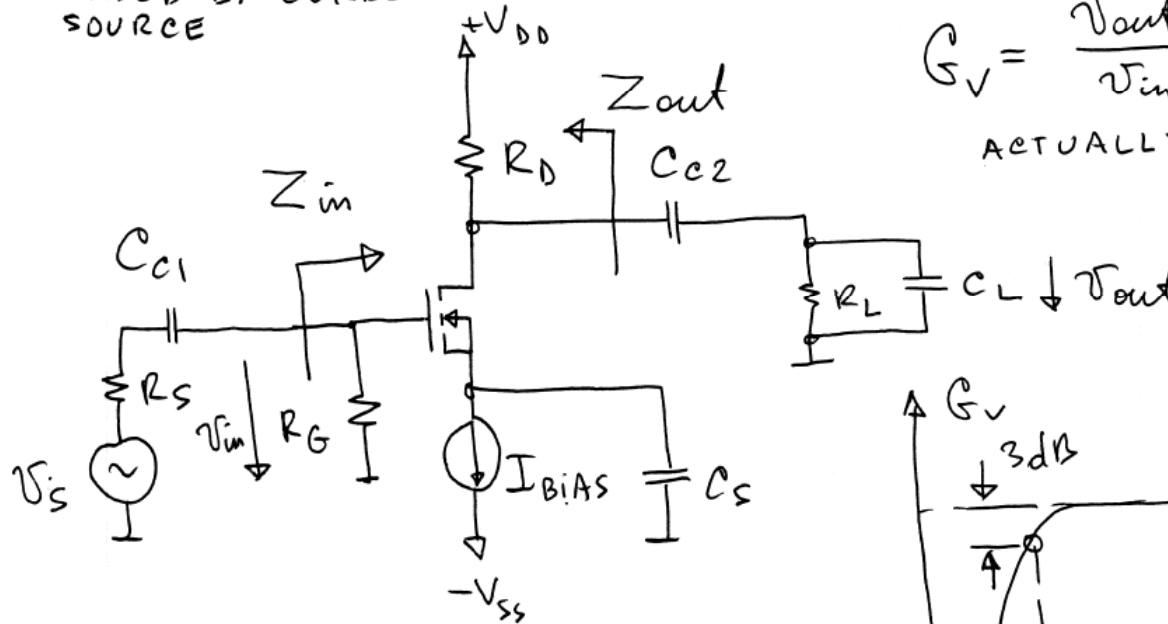


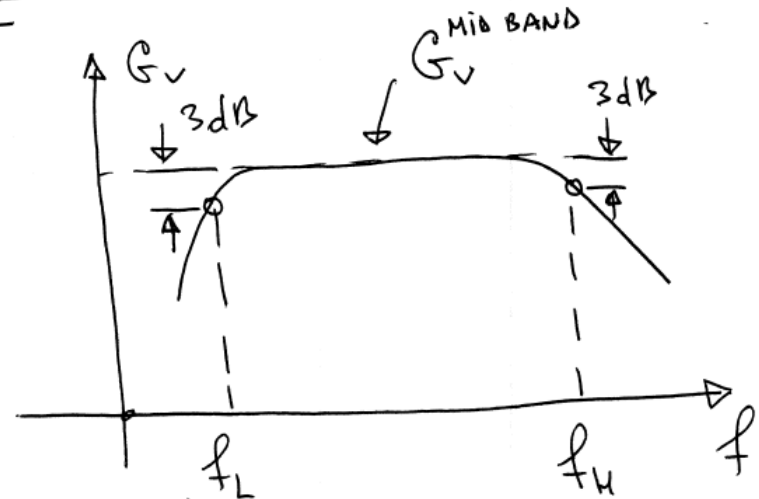
### Frequency response of CS amplifier

CONSIDER CS AMP  
BIASED BY CURRENT  
SOURCE



$$G_V = \frac{v_{out}}{v_{in}} = ?$$

ACTUALLY  $\rightarrow G_V(f)$

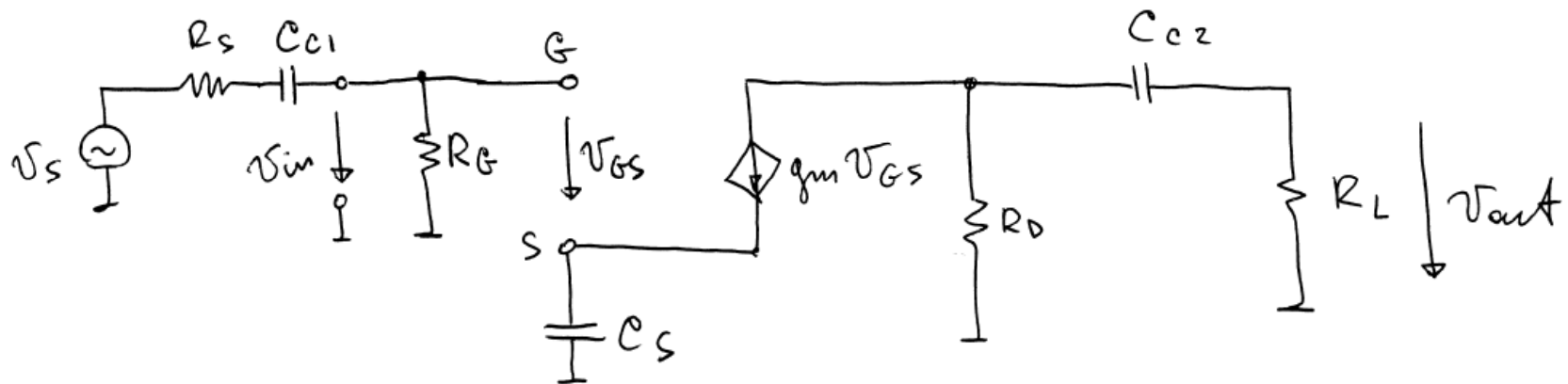
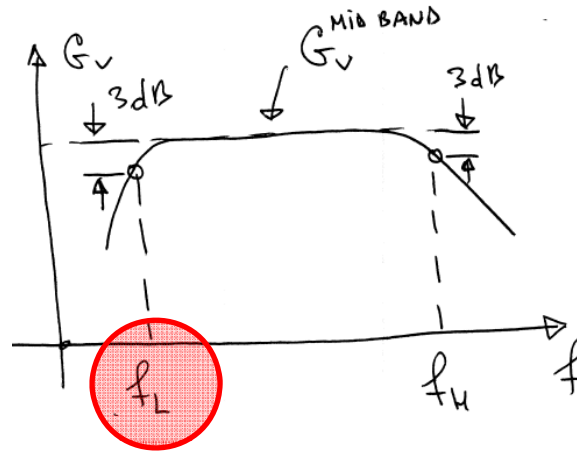


$$G_V^{MID.BAND} = \frac{R_{in}}{R_{in} + R_s} A_{VO} \frac{R_L}{R_L + R_{OUT}}$$

$$R_{in} = R_G ; R_{OUT} = (R_D || r_o) ; A_{VO} = -g_m (R_D || r_o)$$

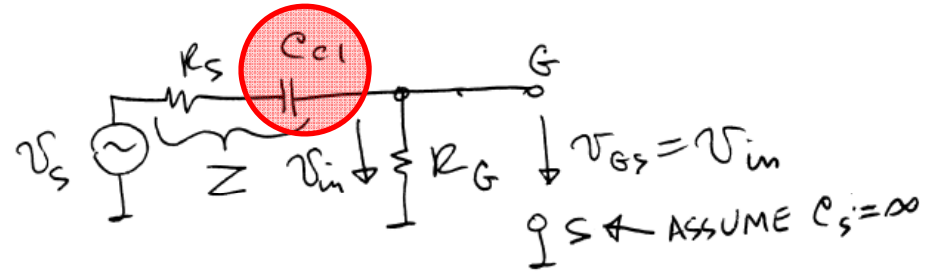
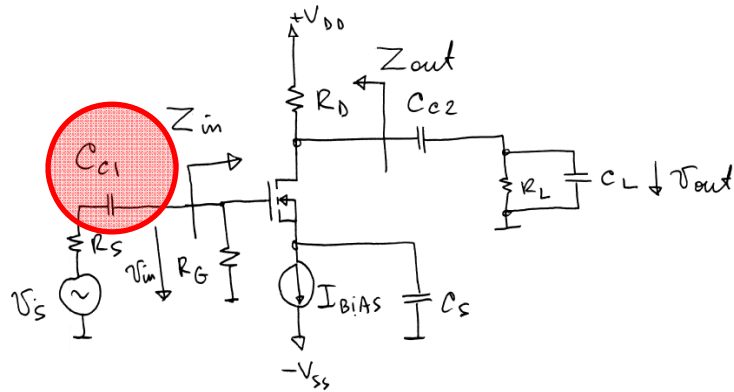
## Low frequency cutoff

*HPF action of coupling and bypass capacitors*



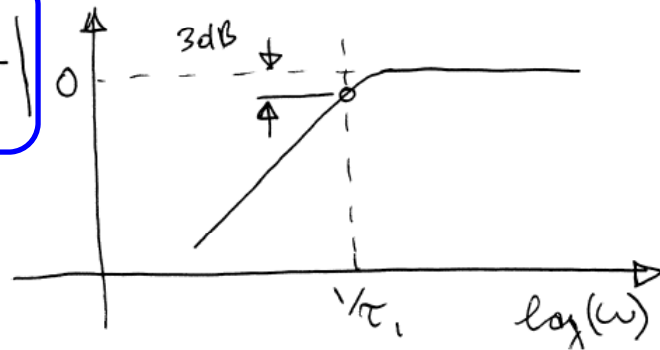
$$G_v(f) = \frac{V_{out}(f)}{V_s(f)} = \underbrace{\frac{V_{out}(f)}{V_{GS}(f)}}_{C_{c2}} \cdot \underbrace{\frac{V_{GS}(f)}{V_{in}(f)}}_{C_s} \cdot \underbrace{\frac{V_{in}(f)}{V_s(f)}}_{C_{c1}}$$

## Effect of $C_{c1}$



$$\begin{aligned} \frac{V_{in}}{V_s} &= \frac{R_G}{R_G + Z} = \frac{R_G}{R_G + R_s + \frac{1}{j\omega C_{c1}}} = \frac{j\omega C_{c1} R_G}{1 + j\omega C_{c1} (R_G + R_s)} = \\ &= \frac{R_G}{R_G + R_s} \cdot \frac{j\omega [(R_G + R_s) C_{c1}]}{1 + j\omega [(R_G + R_s) C_{c1}]} = \frac{R_G}{R_G + R_s} \cdot \frac{j\omega \tau_1}{1 + j\omega \tau_1} \end{aligned}$$

$$20 \log \left| \frac{j\omega \tau_1}{1 + j\omega \tau_1} \right|$$

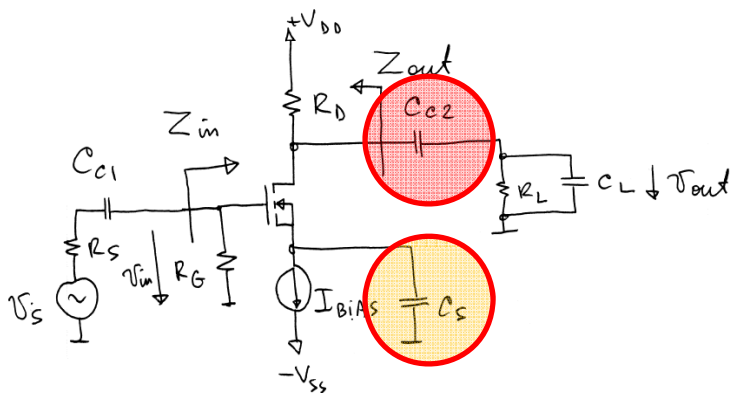


$$\tau_1 = C_{c1} (R_G + R_s)$$

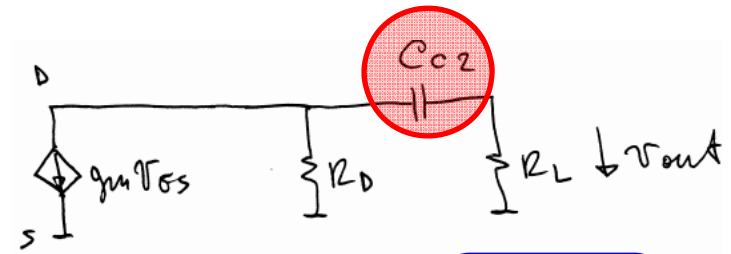
$$f_L \approx \frac{1}{2\pi \tau_1}$$

# Effect of $C_s$ and $C_{c2}$

\*In our labs we will use  $R_G = \infty$  so no need in  $C_{c1}$



## 1. Effect of $C_{c2}$

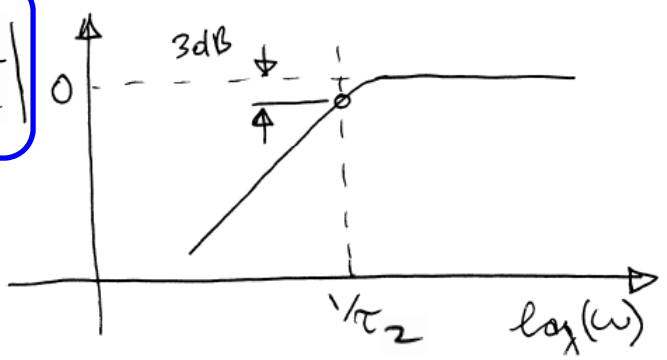


$$\frac{v_{out}}{v_{gs}} = - \frac{g_m v_{gs}}{v_{gs}} \cdot \frac{R_D}{R_D + R_L + \frac{1}{j\omega C_{c2}}} \cdot R_L = -g_m (R_D || R_L)$$

$$\frac{j\omega \tau_2}{1 + j\omega \tau_2}$$

MPF

$$20 \log \left| \frac{j\omega \tau_2}{1 + j\omega \tau_2} \right|$$

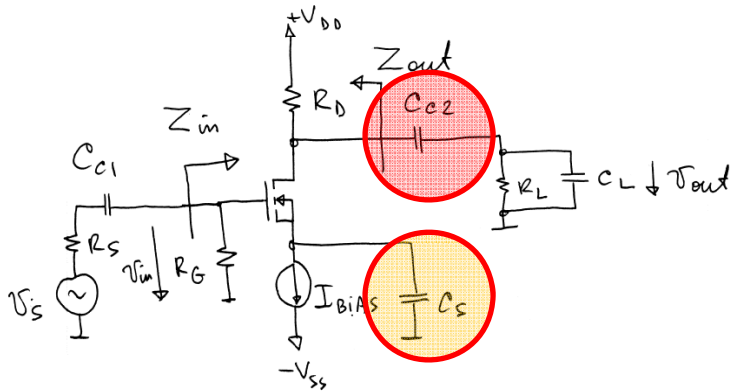


$$\tau_2 = C_{c2} (R_D + R_L)$$

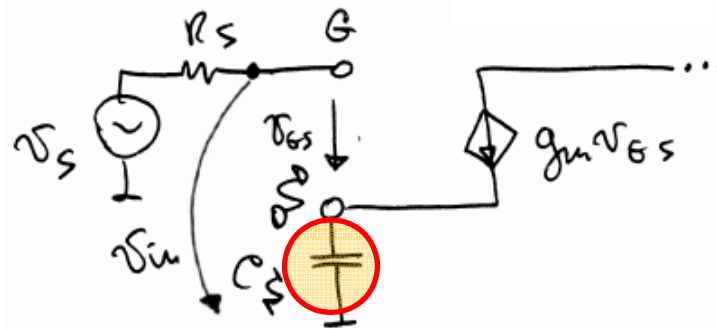
⊛  $C_{c2} = 100 \text{ nF}$   
 $R_D + R_L = 10 \text{ k}\Omega$  }  $\tau_2 = 10^{-7} \cdot 10^4 = 10^{-3} \text{ s} \Rightarrow f_L = \frac{1}{2\pi \cdot 10^{-3}} \approx 160 \text{ Hz}$

# Effect of $C_s$ and $C_{c2}$

\*In our labs we will use  $R_G = \infty$  so no need in  $C_{c1}$



## 1. Effect of $C_s$

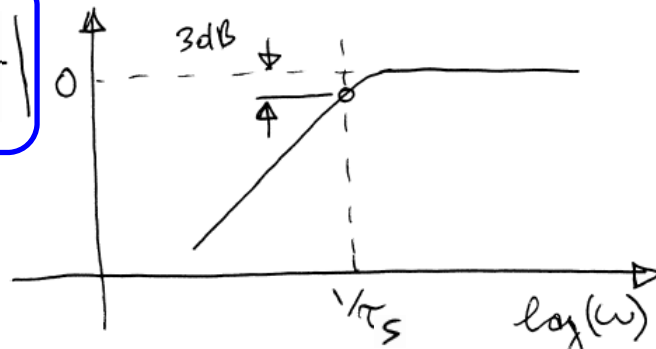


$$\frac{V_{GS}}{V_{in}} = \frac{V_{GS}}{V_{GS} + g_m V_{GS} \frac{1}{j\omega C_s}} = \frac{j\omega \tau_s}{1 + j\omega \tau_s}$$

$\tau_s = C_s / g_m$

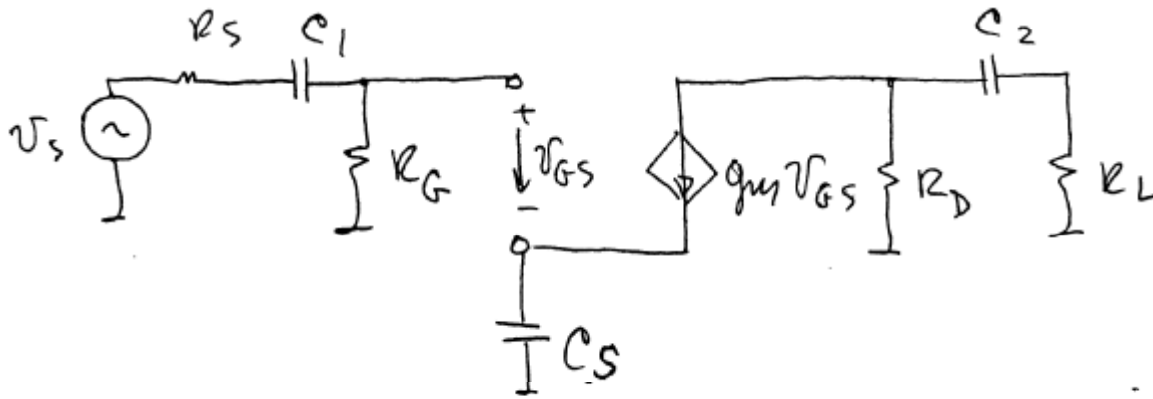
$$\underbrace{\frac{j\omega \tau_s}{1 + j\omega \tau_s}}_{\text{MPF}}$$

$$20 \log \left| \frac{j\omega \tau_s}{1 + j\omega \tau_s} \right|$$



\*  $1/g_m = 1/mA \approx 1k\Omega$

# Open circuit time constants method

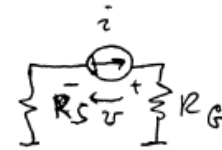


$$f_{co} \approx \frac{1}{2 \cdot \pi \cdot \tau_{\Sigma}}$$

$$\tau_{\Sigma} = \sum_{i=1}^N (C_i \cdot R_i)$$

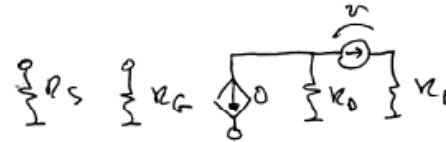
$v_s = 0$   
& look for  $R_i$   
 $C_{j \neq i} = 0$

①.  $\tau_1 = C_1 \cdot R_1 \Rightarrow R_1 = R_s + R_G$

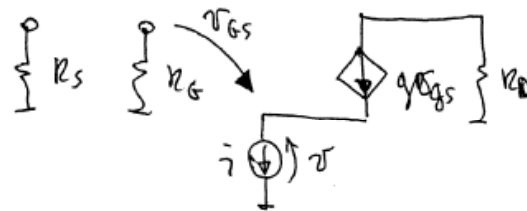


$$v = R_G \cdot i - (-i \cdot R_s)$$

②.  $\tau_2 = C_2 \cdot R_2 \Rightarrow R_2 = R_D + R_L$



③.  $\tau_3 = C_S \cdot R_3 \Rightarrow$

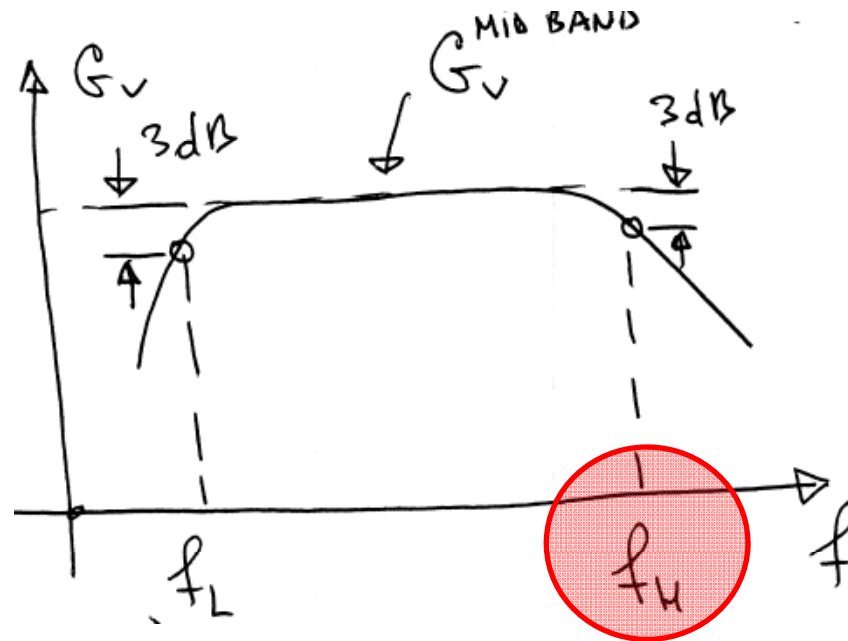


$$i = g_m v_{GS}$$

$$v = v_{GS}$$

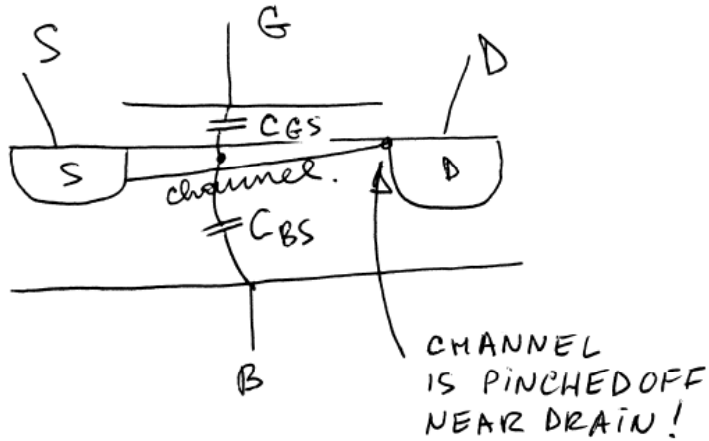
Hence  $R_3 = \frac{v}{i} = \frac{1}{g_m}$

# High frequency cutoff



# High frequency cutoff

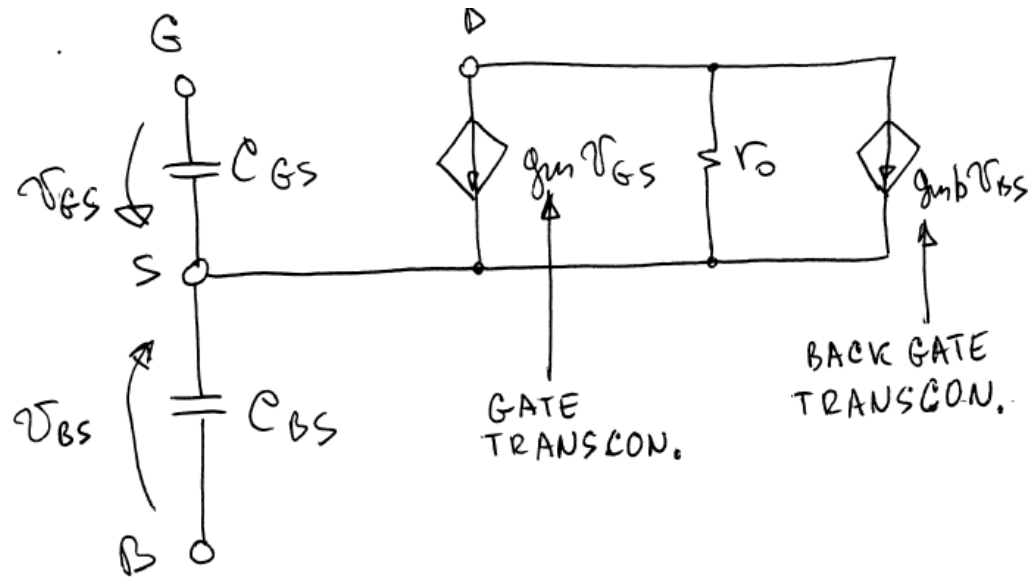
## Intrinsic part in saturation



$$C_{GS} = \frac{2}{3} C_{ox}' \cdot W \cdot L \quad ; \quad C_{ox}' = \frac{\epsilon \epsilon_{ox}}{t_{ox}}$$

$$C_{BS} = \frac{2}{3} C_B \quad \uparrow \text{BODY EFFECT!}$$

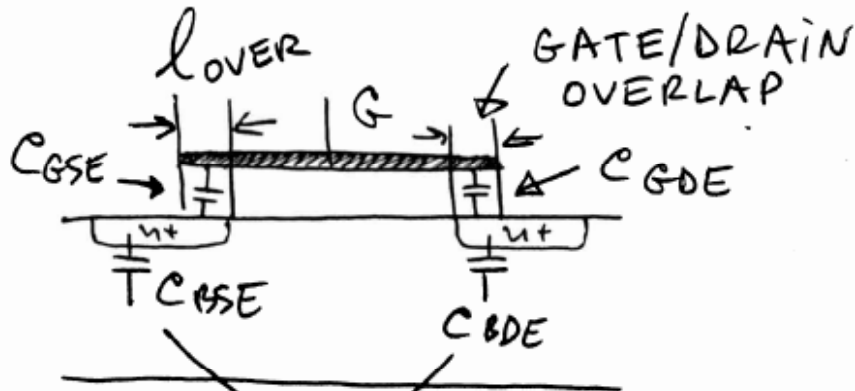
$C_{GS}$  &  $C_{BS}$   
 PRINCIPAL CAPS  
 OF FET





# High frequency cutoff

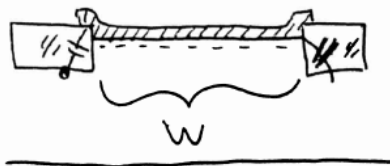
## Extrinsic part



DEPLETION REGION CAPS

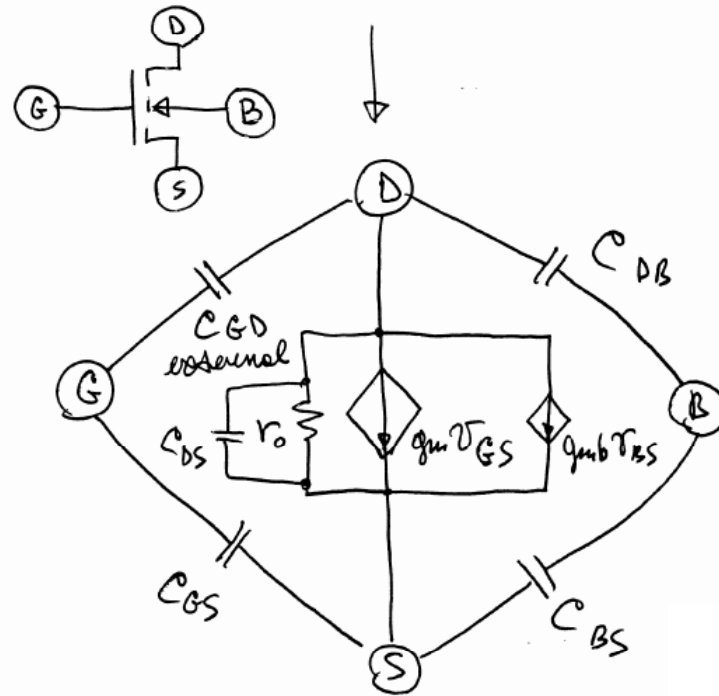
$$C_{depl} = \frac{\epsilon_0 \epsilon_s}{W_{depl}}$$

⊛  $C_{GB}$  - FRINGING CAP

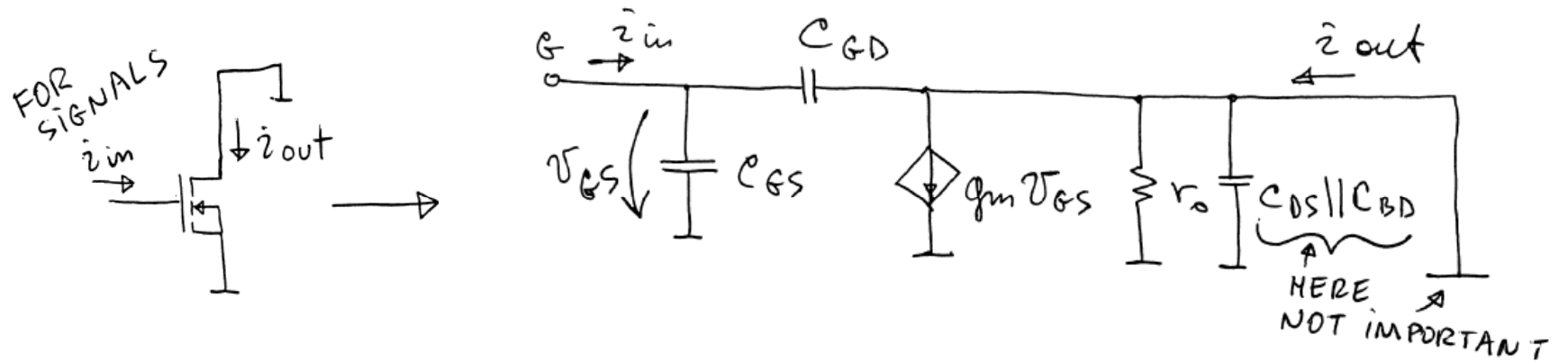


⊛  $C_{DS}$  - PROXIMITY CAP

External (parasitic) and internal (principal) contributions to MOSFET capacitances are in parallel so in saturation:



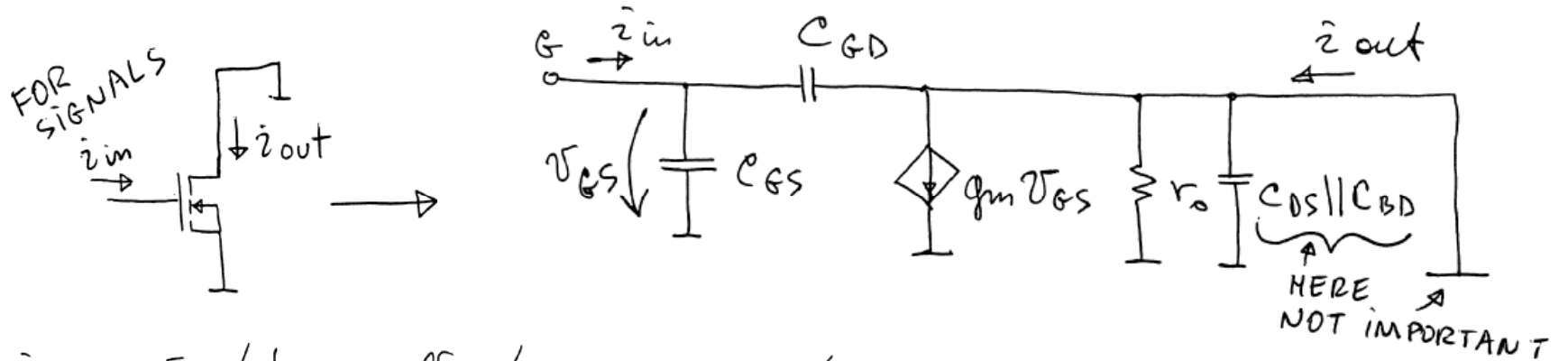
## Short circuit current gain



$$C_{GS} = \underbrace{\frac{2}{3} C_{ox}' \cdot W \cdot L}_{INTERNAL} + \underbrace{C_{ox}' \cdot W \cdot l_{over}}_{EXTERNAL}$$

$$C_{GD} = C_{ox}' \cdot W \cdot l_{over}$$

## Short circuit current gain



$$\tilde{i}_{in} = v_{GS} / \frac{1}{j\omega C_{GS}} + v_{GS} / \frac{1}{j\omega C_{GD}} = j\omega v_{GS} (C_{GS} + C_{GD})$$

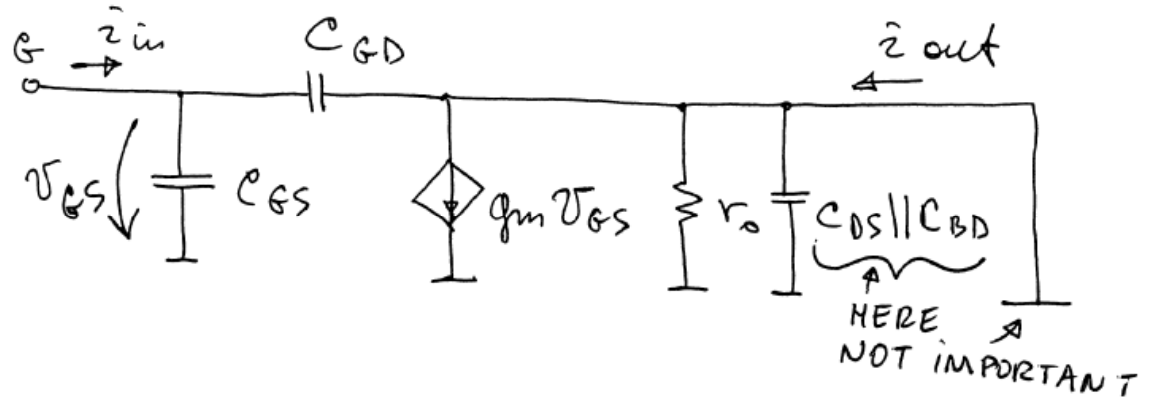
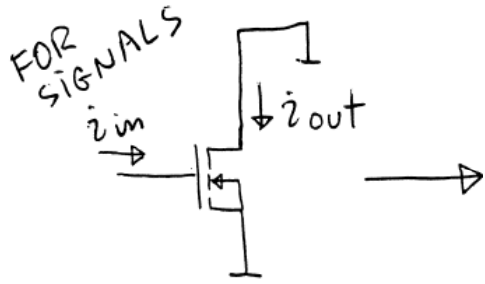
$$\tilde{i}_{out} = g_m v_{GS} - j\omega C_{GD} \cdot v_{GS}$$

$$A_{IO} = \frac{\tilde{i}_{out}}{\tilde{i}_{in}} = \frac{g_m}{j\omega (C_{GS} + C_{GD})} \cdot \frac{1}{1 + C_{GS}/C_{GD}}$$

**Negligible**

$$|A_{IO}(f)| = \frac{g_m}{2\pi f \cdot (C_{GS} + C_{GD})}$$

# Unity gain frequency



$$|A_{IO}(f)| = \frac{g_m}{2\pi f \cdot (C_{GS} + C_{GD})}$$

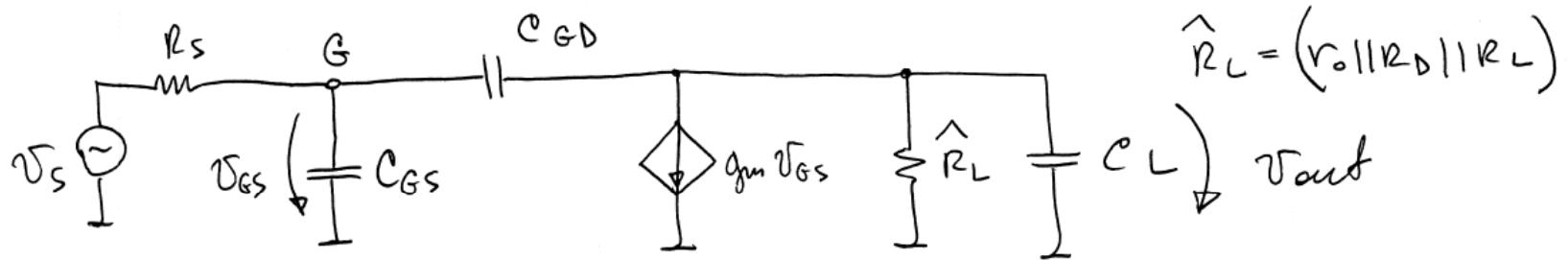
$$|A_{IO}(f_T)| = 1$$

$$f_T = \frac{g_m}{2\pi (C_{GS} + C_{GD})}$$

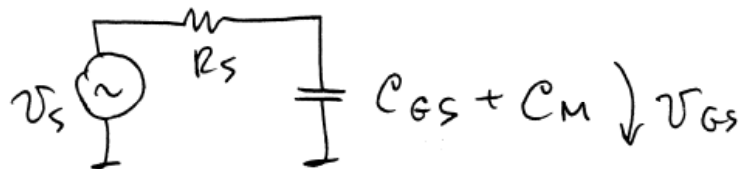
$$f_T = \frac{\frac{W}{L} \mu C_{ox} (V_{GS} - V_T)}{2\pi (W \cdot L \cdot C_{ox} \cdot \frac{2}{3} + W \cdot C_{ox} \cdot l_{over})} = \underbrace{\frac{\mu \cdot (V_{GS} - V_T)}{L}}_{v/L = 1/\tau_{S \rightarrow D}} \cdot \left( \frac{1}{2\pi \left( \frac{2}{3} + \frac{l_{over}}{L} \right)} \right)$$

**Time of flight from source to drain**

# CS amp with load



## 1. Effect of $C_{GS}$ and $C_{GD}$



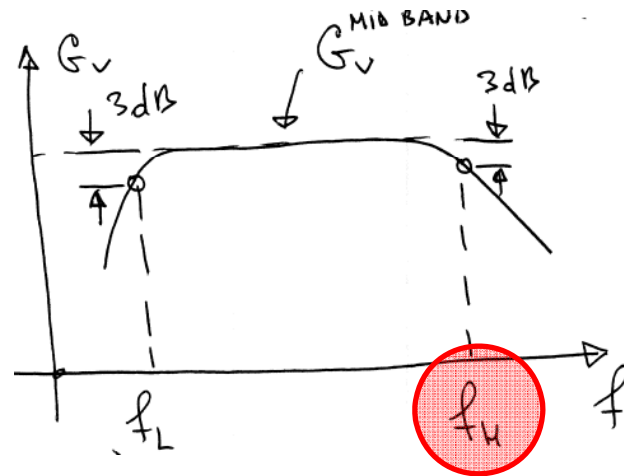
$$\frac{v_{GS}}{v_s} = \frac{1}{1 + j\omega \tau_M}$$

$$\tau_M = R_s (C_{GS} + C_M)$$

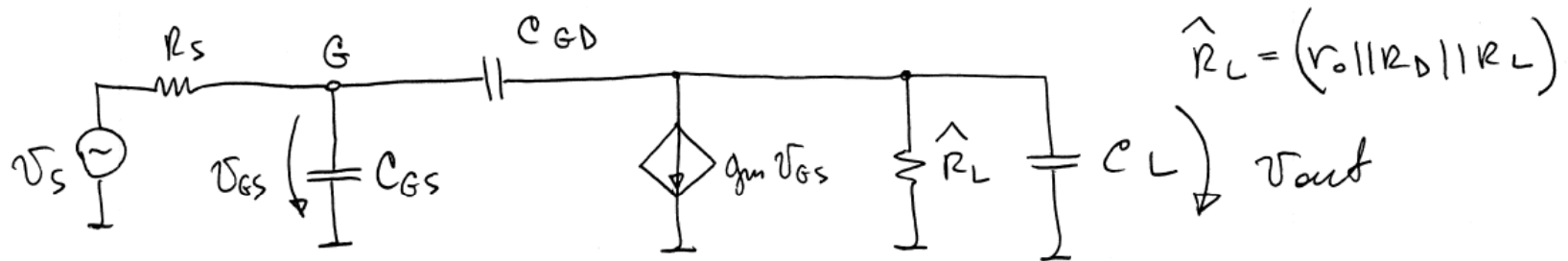
$$f_H \approx \frac{1}{2\pi \tau_M}$$

## Miller cap

$$C_M = (1 + g_m \hat{R}_L) C_{GD}$$

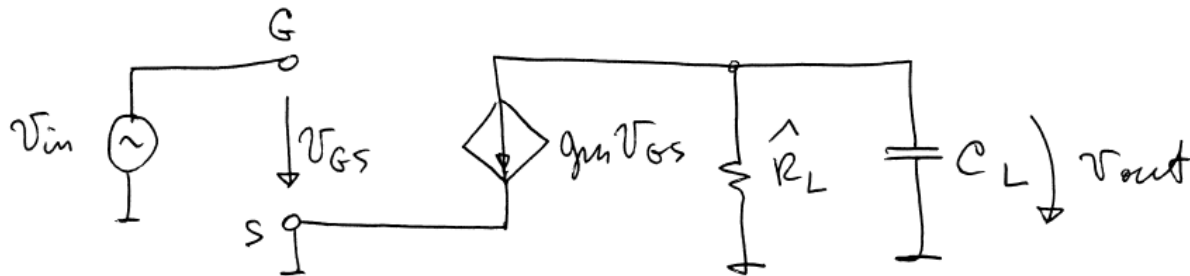


## CS amp with load

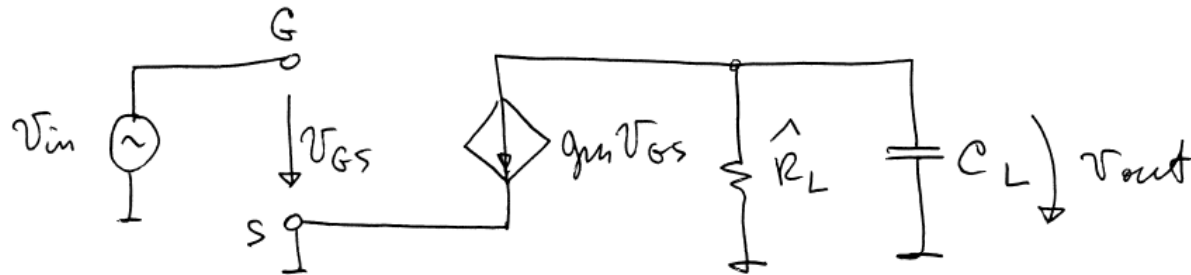


### 1. Effect of $C_L$

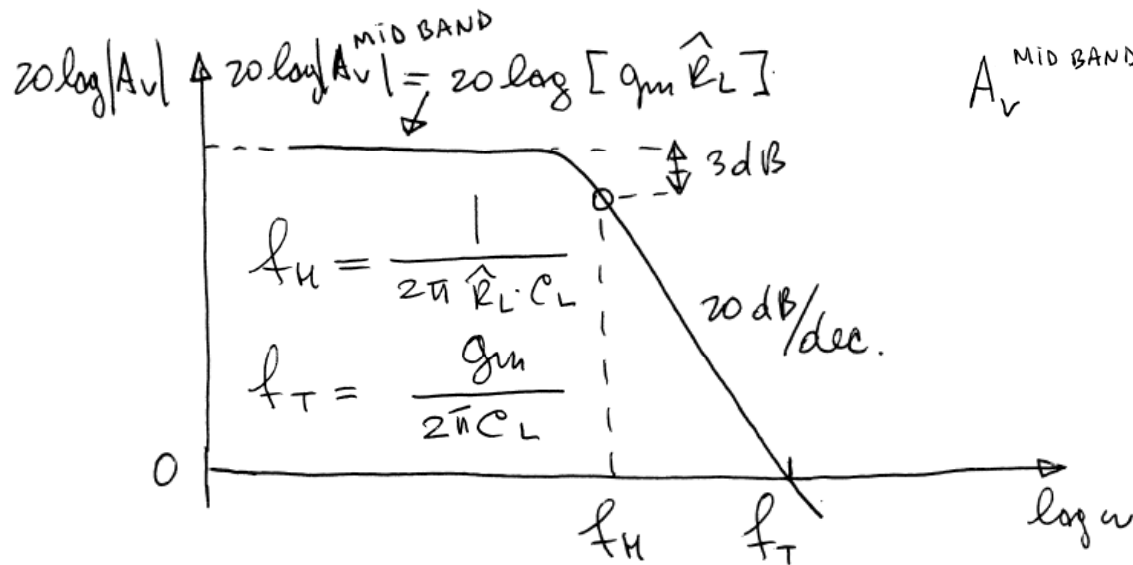
Either assume that role of  $C_{GS}$  and  $C_{GD}$  is not important or measure  $V_{GS}$  directly and treat it as a input signal.



## CS amp with capacitive load



$$A_v(f) = -g_m (\hat{R}_L \parallel C_L) = \frac{-g_m \hat{R}_L}{1 + j\omega [\hat{R}_L \cdot C_L]}$$



$$A_v^{MID\ BAND} \times f_H = f_T = \underline{\underline{G_{max} \cdot BW}}$$

$\star$   $g_m = 1 \frac{\text{mA}}{\text{V}}$   
 $C_L = 20\text{pF}$   
 then  $f_T \approx 8\text{MHz}$

for  $A_v^{m.b} \approx 10 \frac{\text{V}}{\text{V}}$   
 then  $f_H \approx 800\text{kHz}!$